

Acid-Base Equilibria

Chapter 16

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16.3 Autoionization of Water

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Definition of Acids & Bases

Arrhenius Definition:

Base: produces OH^- in aqueous solutions



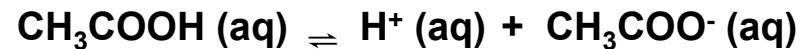
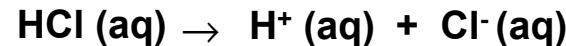
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Definition of Acids & Bases

Arrhenius Definition:

Acid: produces H^+ in aqueous solutions



Acetic acid

Acetate ion



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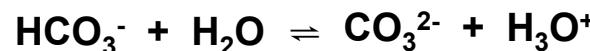
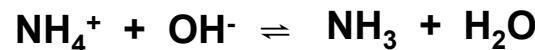
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Definition of Acids & Bases

Brønsted-Lowry Definition:

Acid: proton (H^+) donor

Base: proton (H^+) acceptor



$\text{NH}_3(\text{g})$ is B-L base but not Arrhenius base



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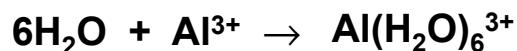
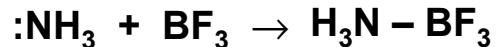
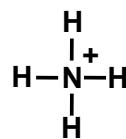
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Definition of Acids & Bases

Lewis Definition:

Acid: electron pair ($2e^-$) acceptor

Base: electron pair ($2e^-$) donor



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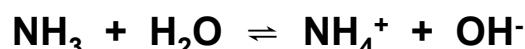
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Conjugate Acid-Base Pairs



HA/A⁻: conjugate acid-base pair

H₃O⁺/H₂O: conjugate acid-base pair



Conjugates: NH₄⁺ / NH₃

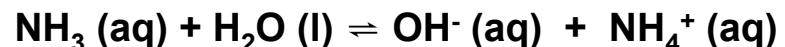
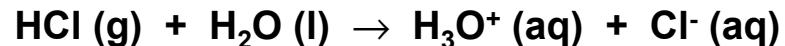
H₂O / OH⁻



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Brønsted-Lowry Acids & Bases



Brønsted-Lowry acid-base reactions are H⁺ transfer reactions.

Brønsted-Lowry acid: must have H⁺ to donate

Brønsted-Lowry base: must have nonbonding e-pair to accept that proton.

H₂O: Amphoteric, can react as an acid or as a base.



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Conjugate Acid-Base Pairs

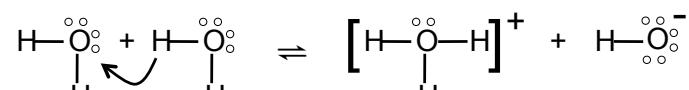
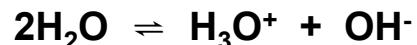
acid	conjugate base	base	conjugate acid
HCO ₃ ⁻	CO ₃ ²⁻	HCO ₃ ⁻	H ₂ CO ₃
OH ⁻	O ²⁻	OH ⁻	H ₂ O
NH ₃	NH ₂ ⁻	F ⁻	HF
H ₂ PO ₄ ⁻	HPO ₄ ²⁻	PO ₄ ³⁻	HPO ₄ ²⁻
PO ₄ ³⁻	??		



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Dissociation of Water



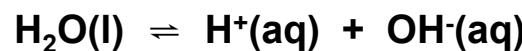
Hydronium ion



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Dissociation of Water



$$K_c = \frac{[\text{H}^+][\text{OH}^-]}{[\text{H}_2\text{O}]} \quad [\text{H}_2\text{O}] = \text{constant}$$

$$K_c [\text{H}_2\text{O}] = K_w = [\text{H}^+][\text{OH}^-]$$

K_w = Ion-product constant

$$K_w = 1.0 \times 10^{-14} \quad \text{only at } 25^\circ\text{C}$$



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Solution is

$[\text{H}^+] = [\text{OH}^-]$ neutral

$[\text{H}^+] > [\text{OH}^-]$ acidic

$[\text{H}^+] < [\text{OH}^-]$ basic

$$K_w = [\text{H}^+][\text{OH}^-]$$

$$K_w = 1.0 \times 10^{-14} \quad 25^\circ\text{C} \quad \text{In any solution}$$



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What is the concentration of OH^- ions in a HCl solution whose hydrogen ion concentration is 1.3 M at 25°C?

$$K_w = [\text{H}^+][\text{OH}^-] = 1.0 \times 10^{-14}$$

$$[\text{OH}^-] = \frac{K_w}{[\text{H}^+]} = \frac{1.0 \times 10^{-14}}{1.3}$$

$$[\text{OH}^-] = 7.7 \times 10^{-15} \text{ M}$$

Is the solution acidic or basic?



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pH Scale

French: *puissance d'hydrogène*
power of hydrogen

$$\text{pH} = -\log[\text{H}^+] \quad [\text{H}^+] = 10^{-\text{pH}}$$

$$\text{pOH} = -\log[\text{OH}^-] \quad [\text{OH}^-] = 10^{-\text{pOH}}$$



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Solution Is At 25°C pH

neutral $[\text{H}^+] = [\text{OH}^-]$ $[\text{H}^+] = 1 \times 10^{-7}$ 7

acidic $[\text{H}^+] > [\text{OH}^-]$ $[\text{H}^+] > 1 \times 10^{-7}$ < 7

basic $[\text{H}^+] < [\text{OH}^-]$ $[\text{H}^+] < 1 \times 10^{-7}$ > 7

As $[\text{H}^+]$ increases pH decreases



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$$[\text{H}^+][\text{OH}^-] = K_w = 1.0 \times 10^{-14} \quad \text{At } 25^\circ\text{C}$$

$$\log[\text{H}^+] + \log[\text{OH}^-] = \log K_w = \log 1.0 \times 10^{-14}$$

$$-\log[\text{H}^+] + (-\log[\text{OH}^-]) = -\log K_w = -\log 1.0 \times 10^{-14}$$

$$\text{pH} + \text{pOH} = \text{p}K_w = 14$$

$$\text{pH} + \text{pOH} = 14$$



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What is the pH of a solution that is 0.10 M in NaOH?

$$\text{pOH} = -\log[\text{OH}^-] = -\log(0.10) = 1.0$$

$$\text{pH} = 14 - \text{pOH} = 14 - 1 = 13$$

OR

$$[\text{H}^+] = \frac{K_w}{[\text{OH}^-]} = \frac{1.0 \times 10^{-14}}{0.10} = 1.0 \times 10^{-13} \text{ M}$$

$$\text{pH} = -\log 1.0 \times 10^{-13} = 13$$



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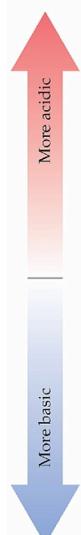
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pH Scale

Can the pH be < 0?

What is the pH of 2 M HCl?

$$\text{pH} = -\log 2 = -0.3$$



	[H ⁺] (M)	pH	pOH	[OH ⁻] (M)
Gastric juice	1 (1×10 ⁻⁰)	0.0	14.0	1×10 ⁻¹⁴
Lemon juice	1×10 ⁻¹	1.0	13.0	1×10 ⁻¹³
Cola, vinegar	1×10 ⁻²	2.0	12.0	1×10 ⁻¹²
Wine	1×10 ⁻³	3.0	11.0	1×10 ⁻¹¹
Tomatoes	1×10 ⁻⁴	4.0	10.0	1×10 ⁻¹⁰
Banana	1×10 ⁻⁵	5.0	9.0	1×10 ⁻⁹
Black coffee	1×10 ⁻⁶	6.0	8.0	1×10 ⁻⁸
Rain	1×10 ⁻⁷	7.0	7.0	1×10 ⁻⁷
Saliva	1×10 ⁻⁸	8.0	6.0	1×10 ⁻⁶
Milk	1×10 ⁻⁹	9.0	5.0	1×10 ⁻⁵
Human blood, tears	1×10 ⁻¹⁰	10.0	4.0	1×10 ⁻⁴
Egg white, seawater	1×10 ⁻¹¹	11.0	3.0	1×10 ⁻³
Baking soda	1×10 ⁻¹²	12.0	2.0	1×10 ⁻²
Borax	1×10 ⁻¹³	13.0	1.0	1×10 ⁻¹
NaOH, 0.1 M	1×10 ⁻¹⁴	14.0	0.0	1 (1×10 ⁻⁰)

pH Scale

Can the pH be > 14?

What is the pH of 10 M NaOH?

$$\text{pOH} = -\log 10 = -1$$

$$\text{pH} = 14 - (-1) = 15$$



	[H ⁺] (M)	pH	pOH	[OH ⁻] (M)
Gastric juice	1 (1×10 ⁻⁰)	0.0	14.0	1×10 ⁻¹⁴
Lemon juice	1×10 ⁻¹	1.0	13.0	1×10 ⁻¹³
Cola, vinegar	1×10 ⁻²	2.0	12.0	1×10 ⁻¹²
Wine	1×10 ⁻³	3.0	11.0	1×10 ⁻¹¹
Tomatoes	1×10 ⁻⁴	4.0	10.0	1×10 ⁻¹⁰
Banana	1×10 ⁻⁵	5.0	9.0	1×10 ⁻⁹
Black coffee	1×10 ⁻⁶	6.0	8.0	1×10 ⁻⁸
Rain	1×10 ⁻⁷	7.0	7.0	1×10 ⁻⁷
Saliva	1×10 ⁻⁸	8.0	6.0	1×10 ⁻⁶
Milk	1×10 ⁻⁹	9.0	5.0	1×10 ⁻⁵
Human blood, tears	1×10 ⁻¹⁰	10.0	4.0	1×10 ⁻⁴
Egg white, seawater	1×10 ⁻¹¹	11.0	3.0	1×10 ⁻³
Baking soda	1×10 ⁻¹²	12.0	2.0	1×10 ⁻²
Borax	1×10 ⁻¹³	13.0	1.0	1×10 ⁻¹
NaOH, 0.1 M	1×10 ⁻¹⁴	14.0	0.0	1 (1×10 ⁻⁰)

Relative Strengths of Acids & Bases

Acid strength: its ability to lose H⁺

Base strength: its ability to gain H⁺

Determined by %ionization or K.

If at the same T and concentration:



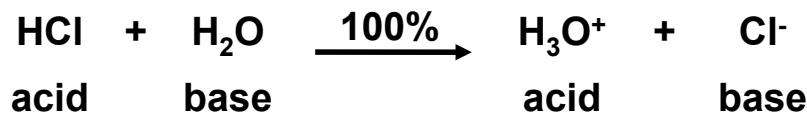
HA stronger acid than HX (larger K_a)



Values of K_a for Some Common Monoprotic Acids

Formula	Name	K _a
HSO ₄ ⁻	Hydrogen sulfate ion	1.2 × 10 ⁻²
HClO ₂	Chlorous acid	1.2 × 10 ⁻²
HF	Hydrofluoric acid	7.2 × 10 ⁻⁴
HNO ₂	Nitrous acid	4.0 × 10 ⁻⁴
CH ₃ COOH	Acetic acid	1.8 × 10 ⁻⁵
HOCl	Hypochlorous acid	3.5 × 10 ⁻⁸
HCN	Hydrocyanic acid	6.2 × 10 ⁻¹⁰
NH ₄ ⁺	Ammonium ion	1.6 × 10 ⁻¹⁰



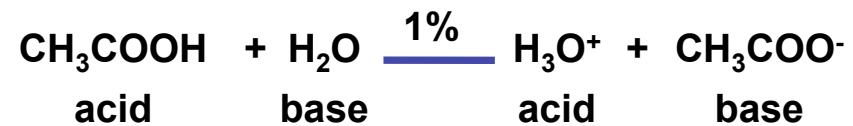


HCl: more ability to loose its H^+ than H_3O^+
HCl stronger acid than H_3O^+

H_2O : accepts H^+ more readily than Cl^-
 H_2O stronger base than Cl^-

Acid strength: $\text{HCl} > \text{H}_3\text{O}^+$

Base strength: $\text{Cl}^- < \text{H}_2\text{O}$



H_3O^+ : more ability to loose its H^+ than H_3COOH
 H_3O^+ stronger acid than CH_3COOH

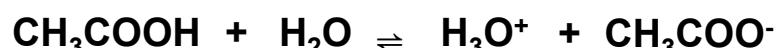
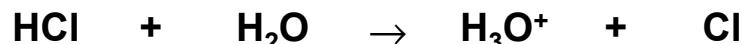
CH_3COO^- : accepts H^+ more readily than H_2O
 CH_3COO^- stronger base than H_2O

Acid strength: $\text{HCl} > \text{H}_3\text{O}^+ > \text{CH}_3\text{COOH}$

Base strength: $\text{Cl}^- < \text{H}_2\text{O} < \text{CH}_3\text{COO}^-$



Important conclusions:



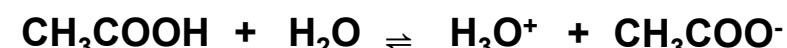
Acid strength: $\text{HCl} > \text{H}_3\text{O}^+ > \text{CH}_3\text{COOH}$

Base strength: $\text{Cl}^- < \text{H}_2\text{O} < \text{CH}_3\text{COO}^-$

1. The stronger the acid, the weaker its conjugate base.



Important conclusions:



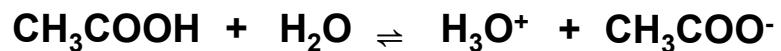
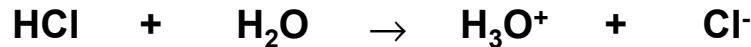
Acid strength: $\text{HCl} > \text{H}_3\text{O}^+ > \text{CH}_3\text{COOH}$

Base strength: $\text{Cl}^- < \text{H}_2\text{O} < \text{CH}_3\text{COO}^-$

2. Strong acid produces no base and weak acid produces weak base.



Important conclusions:



Acid strength: $\text{HCl} > \text{H}_3\text{O}^+ > \text{CH}_3\text{COOH}$

Base strength: $\text{Cl}^- < \text{H}_2\text{O} < \text{CH}_3\text{COO}^-$

3. Acid-base reactions go in the direction of the weaker.



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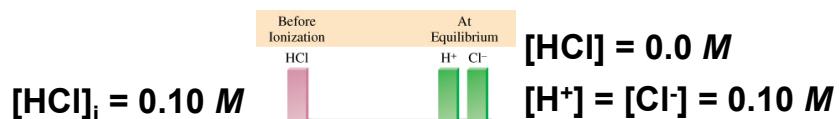
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Strong Acids & Bases

Strong acids you should know:

HCl , HBr , HI , HNO_3 , HClO_3 , HClO_4 .

H_2SO_4 (1st H^+ only).



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H_3O^+ Strongest acid that can exist in aqueous solution

	ACID	BASE	
100% ionized in H_2O	HCl H ₂ SO ₄ HNO ₃	Cl ⁻ HSO ₄ ⁻ NO ₃ ⁻	Negligible
Strong	$\text{H}_3\text{O}^{+}(aq)$	H_2O	
	HSO ₄ ⁻	SO ₄ ²⁻	
	H ₃ PO ₄	H ₂ PO ₄ ⁻	
	HF	F ⁻	
	HC ₂ H ₃ O ₂	C ₂ H ₃ O ₂ ⁻	
	H ₂ CO ₃	HCO ₃ ⁻	
	H ₂ S	HS ⁻	
	H ₂ PO ₄ ⁻	HPO ₄ ²⁻	
	NH ₄ ⁺	NH ₃	
	HCO ₃ ⁻	CO ₃ ²⁻	
	HPO ₄ ²⁻	PO ₄ ³⁻	
	H_2O	OH^-	
Negligible	OH ⁻	O ²⁻	
	H ₂	H ⁻	
	CH ₄	CH ₃ ⁻	
			100% protonated in H_2O

OH^- Strongest base that can exist in aqueous solution

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What is the pH of $2 \times 10^{-3} \text{ M HNO}_3$ solution?

HNO_3 is a strong acid

100% ionization

	$\text{HNO}_3(aq)$	\rightarrow	$\text{H}^+(aq)$	$+$	$\text{NO}_3^-(aq)$
Initial, <i>i</i>	2×10^{-3}		0.0		0.0
Change, Δ	-2×10^{-3}		$+2 \times 10^{-3}$	$+2 \times 10^{-3}$	
Final, <i>f</i>	0.0		2×10^{-3}	2×10^{-3}	

$$\text{pH} = -\log[\text{H}^+]$$

$$\text{pH} = -\log(2 \times 10^{-3})$$

$$\text{pH} = 2.7$$



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What is the pH of $2 \times 10^{-3} M$ HNO₃ solution?

$$[\text{H}^+] = 2.0 \times 10^{-3} M$$

$$[\text{OH}^-] = \frac{K_w}{[\text{H}^+]} = \frac{1.0 \times 10^{-14}}{2.0 \times 10^{-3}} = 5.0 \times 10^{-12} M$$



$$[\text{H}^+]_{\text{water}} = [\text{OH}^-] = 5.0 \times 10^{-12} M$$

In strong acid solutions, ignore [H⁺] from water unless the [acid] $\leq 10^{-6} M$

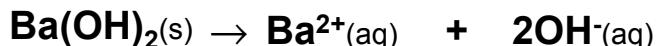


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Calculate the pH of $1.8 \times 10^{-2} M$ Ba(OH)₂ solution.

Ba(OH)₂ is a strong base 100% ionization



$$i \quad 1.8 \times 10^{-2} \quad 0.0 \quad 0.0$$

$$\Delta \quad -1.8 \times 10^{-2} \quad + 1.8 \times 10^{-2} \quad + 2(1.8 \times 10^{-2})$$

$$f \quad 0.0 \quad 1.8 \times 10^{-2} \quad 2(1.8 \times 10^{-2})$$

$$\text{pOH} = -\log (0.036) = 1.4$$

$$\text{pH} = 14 - 1.44 = 12.6$$

Ignore OH⁻ from water



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Strong Acids & Bases

Strong bases you should know:

1. Hydroxides of group I & group II:



2. Oxides: O²⁻(aq) + H₂O → 2OH⁻(aq)

3. Hydrides: H⁻(aq) + H₂O → H₂(g) + OH⁻(aq)

4. Nitrides: N³⁻(aq) + 3H₂O → NH₃(aq) + 3OH⁻(aq)



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Weak Acids



$$[\text{HF}]_i = 0.10 M$$

$$[\text{HF}] < 0.10 M$$

$$[\text{H}^+] = [\text{F}^-] = ?$$

mixture contains H⁺, A⁻, and HA

$$K_a = \frac{[\text{H}^+][\text{A}^-]}{[\text{HA}]} \quad K_a = \text{acid ionization constant}$$



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What is the pH of a 0.50 M HF solution?
(at 25°C). $K_a = 7.1 \times 10^{-4}$

HF(aq)	\rightleftharpoons	$\text{H}^+(\text{aq})$	$+$	$\text{F}^-(\text{aq})$
<i>i M</i>	0.50	0.0		0.0
ΔM	-x	+x		+x
<i>eq M</i>	0.50 - x	x		x

$$K_a = \frac{[\text{H}^+][\text{F}^-]}{[\text{HF}]} \quad 7.1 \times 10^{-4} = \frac{x^2}{0.50 - x}$$



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Check assumption

Assumption valid when:

x is less than 5% of the value from which it is subtracted.

$$\frac{x}{0.50} \times 100\% < 5\%$$

$$\frac{0.019}{0.50} \times 100\% = 3.8\% < 5\% \quad \text{OK}$$

$$x = [\text{H}^+] = [\text{F}^-] = 0.019 \text{ M}$$

$$[\text{HF}] = 0.50 - x = 0.50 - 0.019 = 0.48 \text{ M}$$

$$\text{pH} = -\log [\text{H}^+] = -\log (0.019)$$

$$\text{pH} = 1.72$$



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$$7.1 \times 10^{-4} = \frac{x^2}{0.50 - x}$$

Assumption: If $x \ll 0.50 \text{ M}$

Then $0.50 - x \approx 0.50 \text{ M}$

$$x^2 = (7.1 \times 10^{-4})(0.50)$$

$$x = 0.019 \text{ M}$$



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$$[\text{H}^+]_w = [\text{OH}^-] = \frac{K_w}{[\text{H}^+]}$$

$$[\text{H}^+]_w = \frac{1.0 \times 10^{-14}}{0.019} = 5.3 \times 10^{-13} \text{ M}$$

$$[\text{H}^+]_w \ll [\text{H}^+]_a$$

For a weak acid equilibrium, ignore the dissociation of water unless the acid solution is very dilute or the K_a value for the acid is comparable to that of water



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What is the pH of a 0.050 M HF solution?
(at 25°C). $K_a = 7.1 \times 10^{-4}$

HF(aq)	\rightleftharpoons	$\text{H}^+(\text{aq})$	+	$\text{F}^-(\text{aq})$
i M	0.050	0.0		0.0
ΔM	-x	+x		+x
eq M	0.050 - x	x		x

$$K_a = \frac{[\text{H}^+][\text{F}^-]}{[\text{HF}]} \quad 7.1 \times 10^{-4} = \frac{x^2}{0.050 - x}$$



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$$7.1 \times 10^{-4} = \frac{x^2}{0.050 - x} \quad \text{Assume } x \ll 0.05 \text{ M}$$

$$7.1 \times 10^{-4} \approx \frac{x^2}{0.050} \quad x = 0.006 \text{ M}$$

Check the 5% rule:

$$\frac{0.006}{0.050} \times 100\% = 12\% > 5\% \quad \text{not OK}$$

Must solve quadratic equation



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$$7.1 \times 10^{-4} = \frac{x^2}{0.050 - x}$$

$$x^2 + 7.1 \times 10^{-4}x - 3.6 \times 10^{-5} = 0$$

$$ax^2 + bx + c = 0 \quad x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = 0.0057 \text{ M}$$

$$[\text{H}^+] = x = 0.0057 \text{ M}$$

$$\text{pH} = -\log (0.0057) = 2.24$$



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The pH of a 0.060 M weak monoprotic acid is 3.44. Calculate the K_a of the acid.

	HA	\rightleftharpoons	H^+	+	A^-
i	0.060		0.0		0.0
Δ	-x		+x		+x
eq	0.060 - x		x		x

$$K_a = \frac{[\text{H}^+][\text{A}^-]}{[\text{HA}]} = \frac{x^2}{0.060 - x}$$

$$x = [\text{H}^+] = 10^{-\text{pH}} = 10^{-3.44} = 3.6 \times 10^{-4} \text{ M}$$



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The pH of a 0.060 M weak monoprotic acid is 3.44. Calculate the K_a of the acid.

	HA	\rightleftharpoons	H^+	$+$	A^-
<i>i</i>	0.060		0.0		0.0
Δ	-x		+x		+x
<i>eq</i>	0.060 - x		x		x

$$\text{eq } 0.060 - 3.6 \times 10^{-4} \quad 3.6 \times 10^{-4} \quad 3.6 \times 10^{-4}$$

$$K_a = \frac{[\text{H}^+][\text{A}^-]}{[\text{HA}]} = \frac{(3.6 \times 10^{-4})(3.6 \times 10^{-4})}{0.060 - 3.6 \times 10^{-4}}$$

$$K_a = 2.2 \times 10^{-6}$$



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Percent Ionization

$[\text{HF}]_i$	0.50 M	0.050 M
$[\text{H}^+]$	0.019	0.0057
pH	1.72	2.24
% ionization	3.8%	11.4%

As the concentration of a weak acid solution decreases, $[\text{H}^+]$ decreases, the pH increases, and the percent ionization increases



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Percent Ionization



$$\% \text{ionization} = \frac{[\text{H}^+]}{[\text{HA}]_i} \times 100\%$$

0.50 M HF:

$$\% \text{ionization} = \frac{0.019}{0.50} \times 100\% = 3.8\%$$

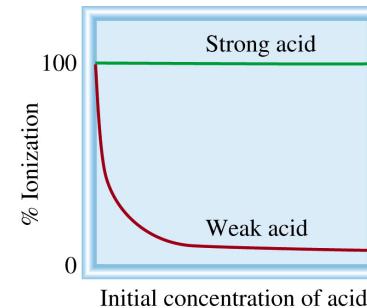
0.050 M HF:

$$\% \text{ionization} = \frac{0.0057}{0.050} \times 100\% = 11.4\%$$



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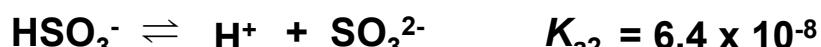


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Polyprotic Acids

Produces more than one H⁺ in solution.



Easier to remove H⁺ from a neutral species than from a negatively charged ion.

ALWAYS: $K_{a1} > K_{a2} > K_{a3} > \dots$

In solution, consider [H⁺] only from first ionization if $K_{a1}/K_{a2} \geq 10^3$.



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$$4.3 \times 10^{-7} = \frac{x^2}{0.040 - x}$$

Using approximation: $x = 1.3 \times 10^{-4} M$

Check: $\frac{1.3 \times 10^{-4}}{0.040} \times 100\% = 0.33\% \quad \text{OK}$

$$x = [\text{H}^+] = [\text{HCO}_3^-] = 1.3 \times 10^{-4} M$$

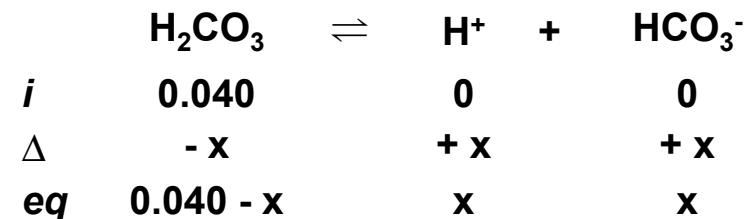
$$\text{pH} = -\log (1.3 \times 10^{-4}) = 3.89$$



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Calculate the concentration of all species present and the pH in a 0.040 M H₂CO₃ acid solution. $K_{a1} = 4.3 \times 10^{-7}$; $K_{a2} = 5.6 \times 10^{-11}$

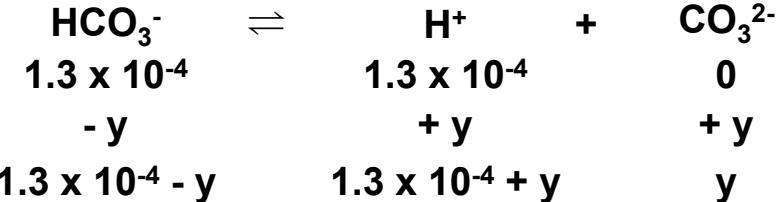


$$K_{a1} = \frac{[\text{H}^+][\text{HCO}_3^-]}{[\text{H}_2\text{CO}_3]} \quad 4.3 \times 10^{-7} = \frac{x^2}{0.040 - x}$$



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$$K_{a2} = \frac{[\text{H}^+][\text{CO}_3^{2-}]}{[\text{HCO}_3^-]}$$

$$5.6 \times 10^{-11} = \frac{(1.3 \times 10^{-4} + y)(y)}{(1.3 \times 10^{-4} - y)}$$

$$y = [\text{CO}_3^{2-}] = 5.6 \times 10^{-11} M = K_{a2}$$

$$y = [\text{H}^+] \text{ from 2nd ionization} = 5.6 \times 10^{-11} M$$



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Weak Bases



Mixture contains: $[HB^+]$, $[OH^-]$, & $[B]$

$$K = \frac{[HB^+][OH^-]}{[H_2O][B]}$$

$$K_b = \frac{[HB^+][OH^-]}{[B]}$$

K_b : base ionization constant
measures the strength of the base



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Calculate the pH of a 0.20 M solution of methylamine, CH_3NH_2 . $K_b = 4.4 \times 10^{-4}$.

	CH_3NH_2	$+ H_2O$	\rightleftharpoons	$CH_3NH_3^+$	$+ OH^-$
<i>i</i>	0.20			0	0
Δ	- x			+ x	+ x
<i>eq</i>	0.20 - x			x	x

$$K_b = \frac{[CH_3NH_3^+][OH^-]}{[CH_3NH_2]} \quad 4.4 \times 10^{-4} = \frac{x^2}{0.20 - x}$$



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Common weak bases

Ammonia and its derivatives:



Conjugate bases for weak acids:



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$$4.4 \times 10^{-4} = \frac{x^2}{0.20 - x}$$

Assume $x \ll 0.20$

$$x = 9.4 \times 10^{-3} M$$

4.7% of 0.20

$$x = [OH^-] = 9.4 \times 10^{-3} M$$

$$pOH = -\log(9.4 \times 10^{-3}) = 2.00$$

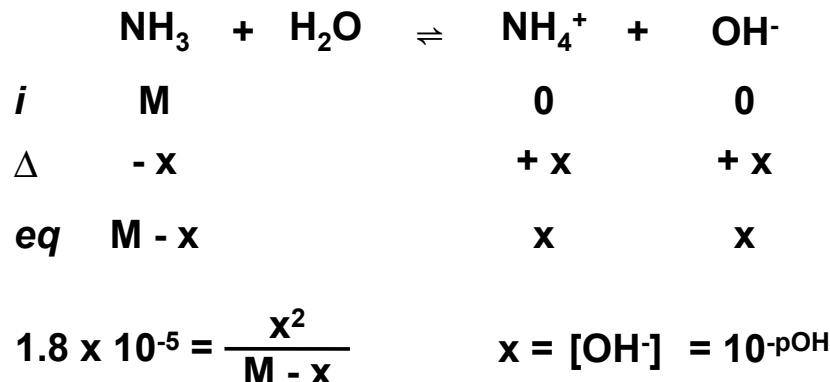
$$pH = 14 - 2.00 = 12$$



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A solution of NH_3 in water has a pH of 10.50. What is the molarity of the solution? $K_b = 1.8 \times 10^{-5}$.



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$$1.8 \times 10^{-5} = \frac{x^2}{M-x} \quad x = [\text{OH}^-] = 10^{-\text{pOH}}$$

$$\text{pOH} = 14 - 10.50 = 3.50$$

$$x = 10^{-3.50} = 3.2 \times 10^{-4} M$$

$$1.8 \times 10^{-5} = \frac{(3.2 \times 10^{-4})^2}{M - 3.2 \times 10^{-4}}$$

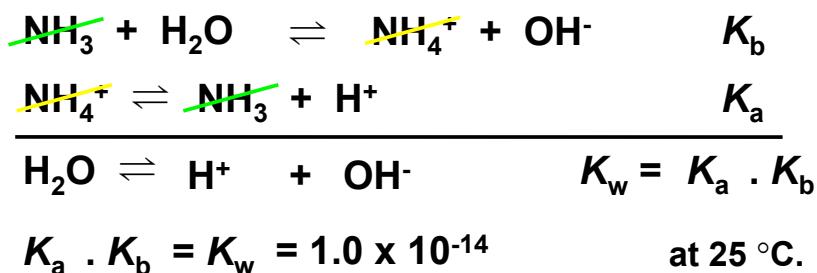
$$M = 6.0 \times 10^{-3} M$$



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K_a - K_b Relationship



The stronger the acid the weaker its conjugate base.

$$K_a = \frac{K_w}{K_b}$$

$$K_b = \frac{K_w}{K_a}$$



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Acid-Base Properties of Salts



If M^+ is conjugate acid for a weak base, its hydrolysis in water will produce H^+ in solution, example NH_4^+ .

If X^- is conjugate base for a weak acid, its hydrolysis will produce OH^- in solution, example NH_3 .



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NaCl Solution

Salt ionization:



Hydrolysis:



Salt of strong acid & strong base: NEUTRAL



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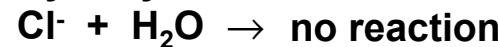
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NH₄Cl Solution

Salt ionization:



Hydrolysis:



Salt of weak base and strong acid: ACIDIC



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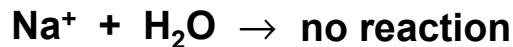
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NaCN Solution

Salt ionization:



Hydrolysis:



Salt of weak acid & strong base: BASIC



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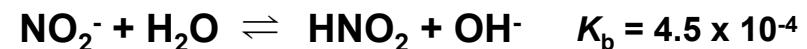
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NH₄NO₂ Solution

Salt ionization:



Hydrolysis:



$$K_b > K_a \quad \text{Basic}$$

Salt of weak acid & weak base:

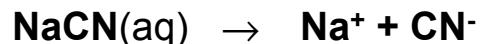
DEPENDS ON K_a & K_b VALUES



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Calculate the pH of a 0.10 M NaCN solution. K_a (HCN) = 4.9×10^{-10} .



$\text{Na}^+ + \text{H}_2\text{O} \rightarrow$ No reaction

	$\text{CN}^- + \text{H}_2\text{O} \rightleftharpoons \text{HCN} + \text{OH}^-$	K_b
<i>i</i>	0.10	0 0
Δ	-x	+x +x
<i>eq</i>	0.10 - x	x x

$$K_b = \frac{K_w}{K_a} = \frac{1.0 \times 10^{-14}}{4.9 \times 10^{-10}} = 2.0 \times 10^{-5}$$



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Calculate the $[\text{H}^+]$ in 1.0 M Na_2CO_3 solution.

H_2CO_3 : $K_{a1} = 4.3 \times 10^{-7}$; $K_{a2} = 5.6 \times 10^{-11}$.



$$K_{b1} = \frac{K_w}{K_{a2}} = \frac{1.0 \times 10^{-14}}{5.6 \times 10^{-11}} = 1.8 \times 10^{-4}$$

$$K_{b2} = \frac{K_w}{K_{a1}} = \frac{1.0 \times 10^{-14}}{4.3 \times 10^{-7}} = 2.3 \times 10^{-8}$$

$$\frac{K_{b1}}{K_{b2}} = \frac{1.8 \times 10^{-4}}{2.3 \times 10^{-8}} = 7.8 \times 10^3$$

Ignore 2nd ionization for $[\text{OH}^-]$ calculations



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	$\text{CN}^- + \text{H}_2\text{O} \rightleftharpoons \text{HCN} + \text{OH}^-$	
<i>i</i>	0.10	0 0
Δ	-x	+x +x
<i>eq</i>	0.10 - x	x x

$$K_b = 2.0 \times 10^{-5} = \frac{x^2}{0.10 - x}$$

$$x = [\text{OH}^-] = 1.4 \times 10^{-3} \text{ M} \quad < 5\%$$

$$\text{pOH} = -\log (1.4 \times 10^{-3}) = 2.85$$

$$\text{pH} = 14 - 2.85 = 11.15$$



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<i>i</i>	1.0	0.0	0.0
Δ	-x	+x	+x
<i>eq</i>	1.0 - x	x	x

$$K_{b1} = 1.8 \times 10^{-4} = \frac{x^2}{1.0 - x}$$

$$x = 0.0134 \text{ M} = [\text{OH}^-] \quad 1.34\%$$

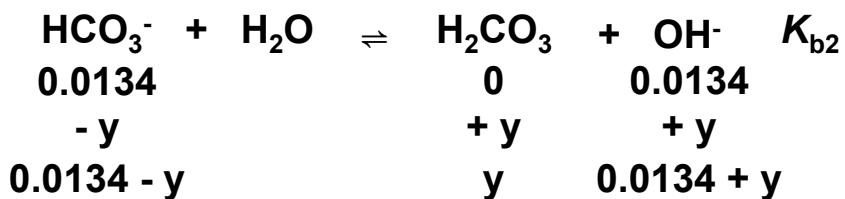
$$[\text{H}^+] = \frac{K_w}{[\text{OH}^-]} = \frac{1.0 \times 10^{-14}}{0.0134} = 7.5 \times 10^{-13} \text{ M}$$

$$[\text{H}_2\text{CO}_3] = ?$$



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$$K_{b2} = \frac{K_w}{K_{a1}} = \frac{1.0 \times 10^{-14}}{4.3 \times 10^{-7}} = 2.3 \times 10^{-8}$$

$$K_{b2} = 2.3 \times 10^{-8} = \frac{(y)(0.0134 + y)}{0.0134 - y}$$

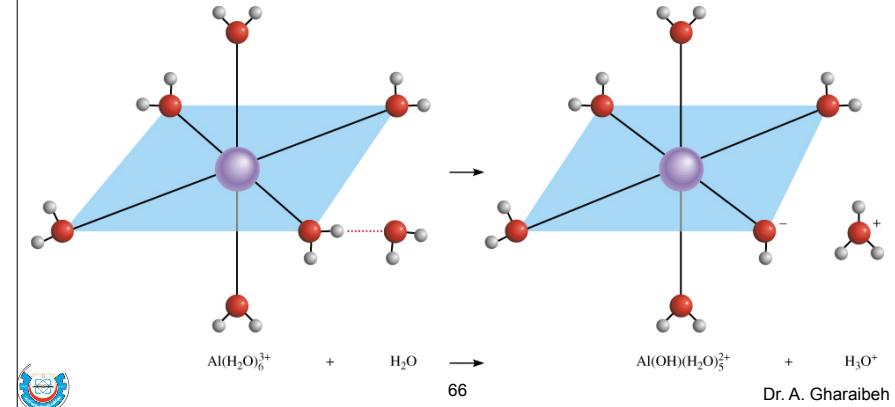
$$y = 2.3 \times 10^{-8} M = K_{a2}$$

$$[\text{H}_2\text{CO}_3] = 2.3 \times 10^{-8} M$$

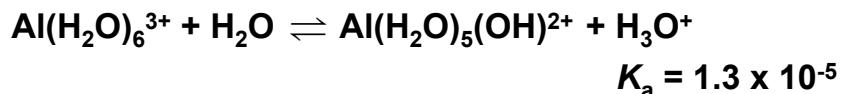


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Hydrolysis of Metal Ions



K_a generally increases with:

1. Increasing metal charge
2. decreasing size of the ion

1 M soln. of $\text{Al}(\text{NO}_3)_3$ $\text{Zn}(\text{NO}_3)_2$ $\text{Ca}(\text{NO}_3)_2$ NaNO_3

pH	3.5	5.5	6.9	7
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